$\qquad$

## Rate of Change

1. 

- Remember the formula distance $=$ rate $\times$ time or $d=r t$ ?
- Consider traveling for 4 hours driving 200 miles
- We can let $\mathrm{d}=200 \& \mathrm{t}=4$, then solve the equation $200=r^{*} 4$ to find that $r=50$.
- Thus, we say that the average speed for the trip was 50 miles per hour. We'll find more average speeds, or rates of change, in this activity.

The data below indicates the time and position of two students racing down the hallway.

| Time (sec.) | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :--- | :--- | :--- | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: |
| Dwain's position (ft.) | 0 | 4 | 8 | 12 | 16 | 20 | 24 | 28 | 32 | 36 | 40 |
| Beth's position (ft.) | 0 | 1 | 3 | 6 | 10 | 15 | 20 | 25 | 30 | 35 | 40 |

a. Draw a graph for this data. Should you connect the dots? Explain.

b. $\qquad$ depends on $\qquad$ . Thus, $\qquad$ is the
independent variable \& $\qquad$ is the dependent variable.
c. Describe how Dwain should walk in order to match his data. In particular, should Dwain's speed be constant or changing/variable?
d. Describe how Beth should walk in order to match her data. In particular, should Beth's speed be constant or changing/variable?

To find average speed, or average rate of change, we use our formula, $\mathrm{d}=\mathrm{rt}$.

Average Rate of Change $=$ change in distance $/$ change in time

When discussing functions with y depending on x ,
Average Rate of Change $=$ change in $y /$ change in $x$
2. Fill in the table:

| $\mathrm{t}(\mathrm{secs})$ | 1 | 2 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| $\mathrm{~d}(\mathrm{t})=\mathrm{t}$ |  |  |  |  |


| $t(\operatorname{secs})$ | 1 | 2 | 3 | 4 |
| :---: | :--- | :--- | :--- | :--- |
| $p(t)=t^{2}$ |  |  |  |  |

a. Find the rate of change for $d(t) \& p(t)$ for each time interval.
$1-2$ seconds:
$2-3$ seconds:

3-4 seconds:
b. What do you notice about the rates of change for the two functions?
c. What is the shape of a graph when the rate of change is constant? variable?
3. Answer the following questions about the graph below.

a. On what intervals is the rate of change positive?
b. On what intervals is the rate of change negative?
c. On what intervals is the rate of change zero?
d. On what interval is the rate of change the largest?
e. On what interval is the rate of change the smallest?

